Routine incorporation of Spatial Covariates into Analysis of Planned Field Experiments

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A Road in Auvers After the Rain by Vincent Van Gogh

Goal: Make everyone feel more comfortable using spatial stats when analyzing field experimental data. (you don't have to be a geospatial statistics expert)

Where to Find This Information

This Presentation:

https://github.com/IdahoAgStats/lattice-spatial-analysis-talk

A longer tutorial:

https://idahoagstats.github.io/guide-to-field-trial-spatial-analysis

What Are Barriers to Using Spatial Stats?

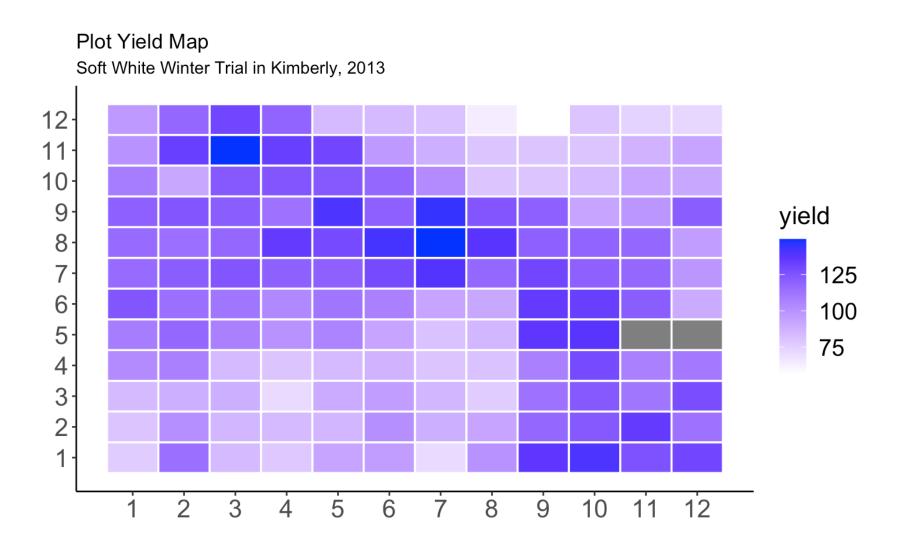
- Perceived lack of need
- Unsure of benefits
- No training in the topic/intimidated by the statistical methodology
- Limited time to devote to statistical analysis
- Unclear what would happen to blocking if spatial stats are used
- very few resources for easy implementation

Spatial Variation in Agricultural Fields

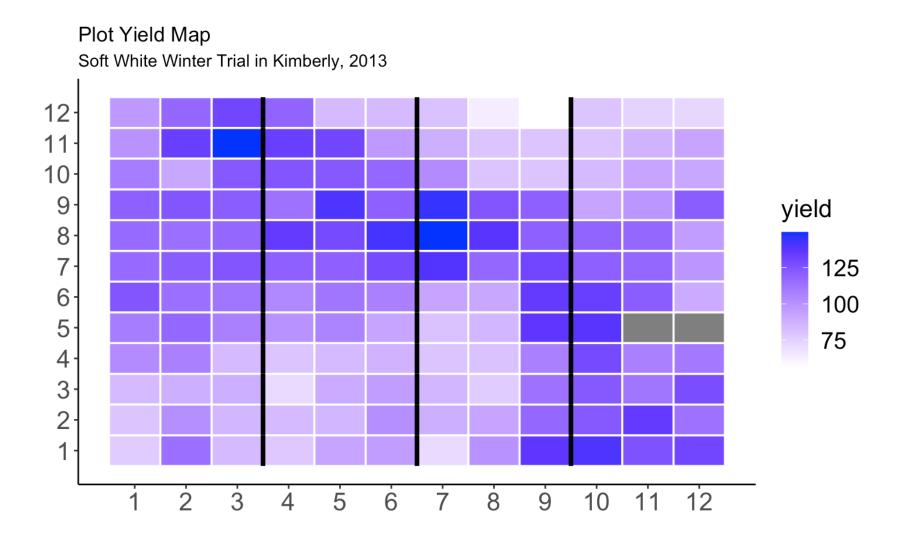


Univeristy of Idaho's Parker Farm (Moscow, Idaho)

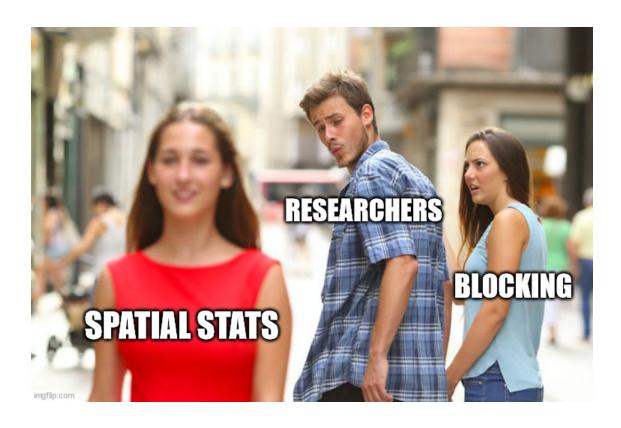
Spatial Variation in Agricultural Fields



Blocking in Agricultural Fields



Blocking versus Spatial Analysis



This is not how this works. Blocking **is** compatible with spatial analysis and recommended for most (all?) field trials.

There Are Many Spatial Methods Available

correlated	l error mod	lels
	correlated	correlated error mod

row and column trend exponential

nearest neighbor spherical

separable ARxAR models Gaussian

spatial error model Matern

spatial lag model Cauchy

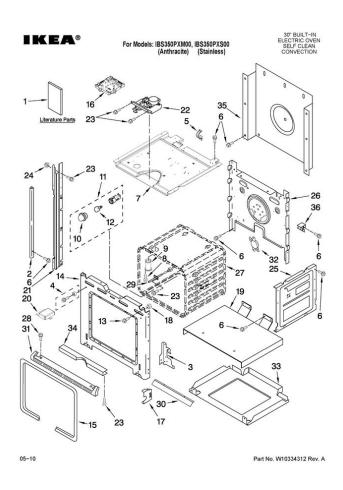
ARIMA power

splines linear

GAMs many more...

These Methods Work

These Methods Can Be Complex



....But

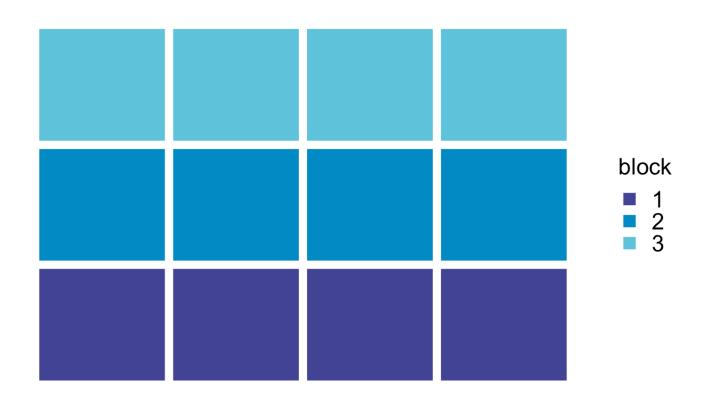
You can also integrate spatial methods into gridded field trials without:

- having to know anything about map projections, shapefiles or other geospatial terminology
- 2. possessing a deep understanding of linear modeling techniques or empirical variograms
- 3. being an R or SAS programming expert

Knowing these things is helpful, but not essential.

A Typical Experiment

- Experimental treatments
- fully crossed effects
- Blocking scheme along the expected direction of field variation



Analysis

A typical linear model:

$$Y_{ij} = \mu + \alpha_i + \beta_j + \epsilon_{ij}$$

Response = trial mean + treatment effect + block effect + leftover error

We Assume:

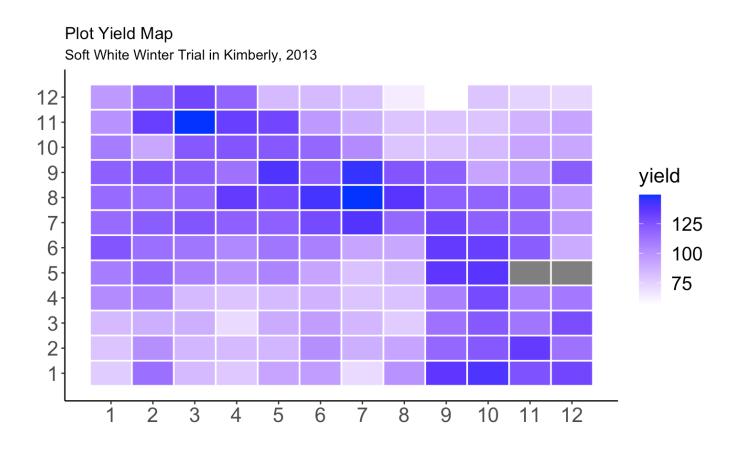
1. The error terms, or residuals, are independent of another with a shared distribution:

$$\epsilon_i \sim N(0,\sigma_e)$$

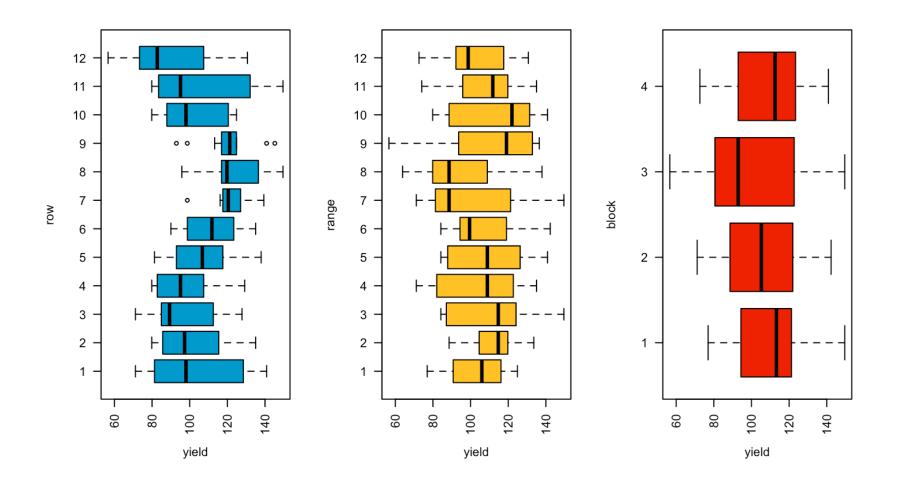
1. Each block captures variation unique to that block and there is no other variation related to spatial position of the experimental plots.

How often is #2 evaluated?

Example Analysis



Average Yield by Row, Column and Block



Standard Analysis of Kimberly, 2013 Wheat Variety Trial

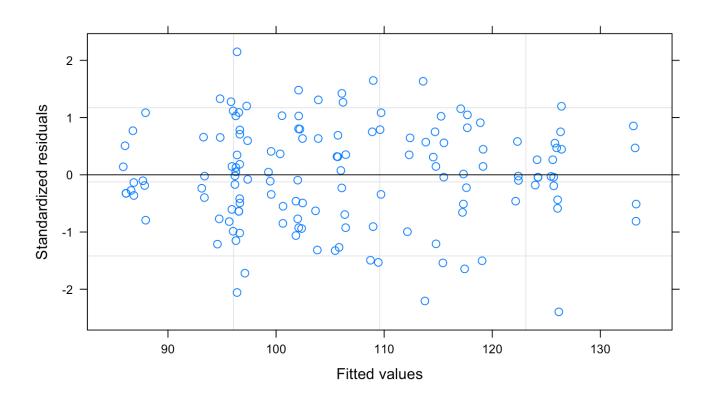
- 36 soft white winter wheat cultivars
- 4 blocks
- · 2 missing data points
- the linear model:

$$Y_{ij} = \mu + \alpha_i + \beta_j + \epsilon_{ij}$$

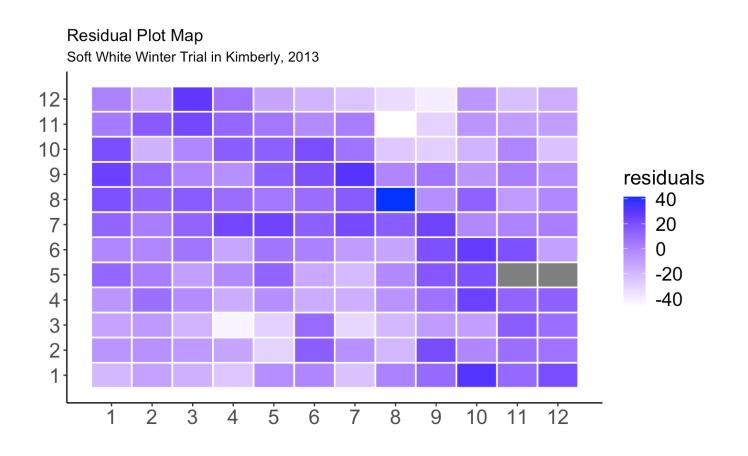
```
library(nlme) lm1 <- lme(yield \sim cultivar, random = \sim 1|block, data = mydata, na.action = na.exclude)
```

What Do The Residuals Look Like?

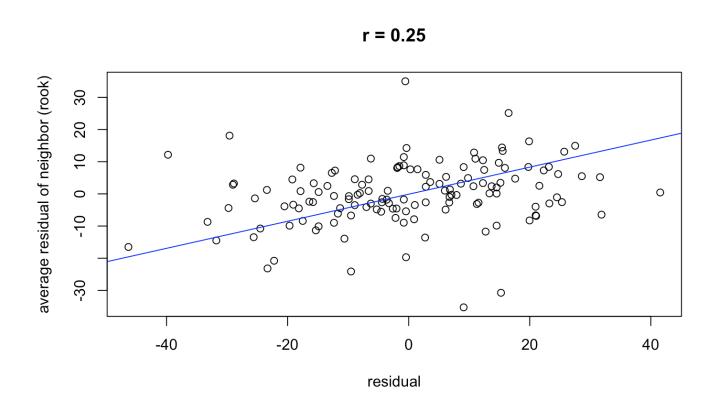
plot(lm1)



What Do The Residuals Look Like Spatially?



What Do The Residuals Look Like Spatially?



Global Moran's Test for Spatial Autocorrelation

 H_0 : There is no spatial autocorrelation

 $H_a:$ There is spatial autocorrelation!

This uses a simple weighting matrix that weights all neighbors that share a plot border (the chess-based "rook" formation) equally.

```
##
## Monte-Carlo simulation of Moran I
##
## data: mydata$residuals
## weights: weights
## omitted: 88, 97
## number of simulations + 1: 1000
##
## statistic = 0.15869, observed rank = 999, p-value = 0.001
## alternative hypothesis: greater
```

Handling Spatial Autocorrelation in Areal Data

Areal data = finite region divided into discrete sub-regions (plots) with aggregated outcomes

Options:

- 1. model row and column trends
 - good for known gradients (hill slope, salinity patterns)
- 2. assume plots close together are more similar than plots far apart. The errors terms can be modelled based on proximity, but there is no trial-wide trend
 - autoregressive models (AR)
 - models utilizing "gaussian random fields" for continuously varying data (e.g. point data)
 - Smoothing splines
 - nearest neighbor

Basic Linear Model

$$Y_{ij} = \mu + A_i + \epsilon_{ij}$$
 $\epsilon_i \sim N(0,\sigma)$

If N = 4:

$$e_i \ \sim Nigg(0, egin{bmatrix} \sigma^2 & 0 & 0 & 0 \ 0 & \sigma^2 & 0 & 0 \ 0 & 0 & \sigma^2 & 0 \ 0 & 0 & 0 & \sigma^2 \end{bmatrix}igg)$$

The variance-covariance matrix indicates a shared variance and all off-diagonals are zero, that is, the errors are uncorrelated.

Linear Model with Autoregressive (AR) Errors

Same linear model:

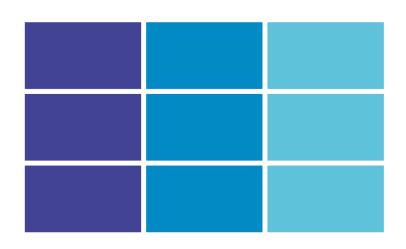
$$Y_{ij} = \mu + A_i + \epsilon_{ij}$$

Different variance structure:

$$e_i \ \sim Nigg(0, = \sigma^2 egin{bmatrix} 1 &
ho &
ho^2 &
ho^3 \
ho & 1 &
ho &
ho^2 \
ho^2 &
ho & 1 &
ho \
ho^3 &
ho^2 &
ho & 1 \end{bmatrix}igg)$$

- ρ is a correlation parameter ranging from -1 to 1 where 0 is no correlation and values approaching 1 indicate spatial correlation.
- The "one" in AR1 means that only the next most adjacent point is considered. There can be AR2, AR3, ..., ARn models.

The Separable AR1 x AR1 model



- AR1xAR1 assumes correlation in two directions, row and column.
- · It estimates σ , ho_{column} , and ho_{row}
- often a good choice since plot are rectangular and hence autocorrelation will differ by direction ("anistropy")

More Notes on Separable AR1xAR1

- From a statistical standpoint, it's one of the more intuitive models
- The implementation in R is a little shaky
 - several packages, all hard to use and incompatible with other R packages
- It is implemented in SAS
- Some proprietary software implements this (AsREML), others do not (Agrobase)

Semivariance and Empirical Variograms

A measure of spatial correlation based on all pairwise correlations in a data set, binned by distance apart:

$$\gamma^2(h)=rac{1}{2}Var[Z(s+h)-Z(s)]$$

Z(s) = observed data at point s.

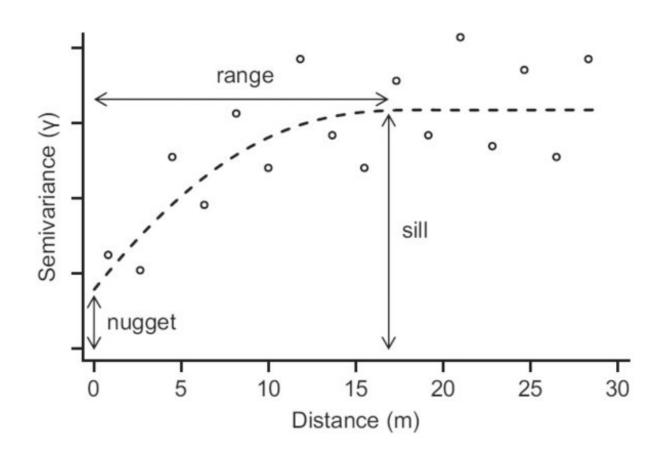
Z(s) = observed data at another point h distance from point s.

For a data set with N observation, there are this many pairwise points:

$$\frac{N(N{-}1)}{2}$$

Empirical Variogram

This uses semivariance to mathematically relate spatial correlations with distance



range = distance up to which is there is spatial correlation sill = uncorrelated variance of the variable of interest nugget = measurement error, or short-distance spatial variance and other unaccounted for variance

Semivariance & Empirical Variograms

- There are many difference mathematical models for explaining semivariance:
 - exponential, Gaussian, Matérn, spherical, ...
- It is usually used for kriging, or prediction of a new point through spatial interpolation
- It can also be used in a linear model where local observations are used to predict a data point in addition to treatment effects
- Bonus: R and SAS are really good at this!

Copy data into new object so we can assign it a new class (and remove missing data):

```
library(gstat); library(sp); library(dplyr)
mydata_sp <- mydata %>% filter(!is.na(yield))
```

Establish coordinates for data set to make it an sp object ("spatial points"):

```
coordinates(mydata_sp) <- ~ row + range</pre>
```

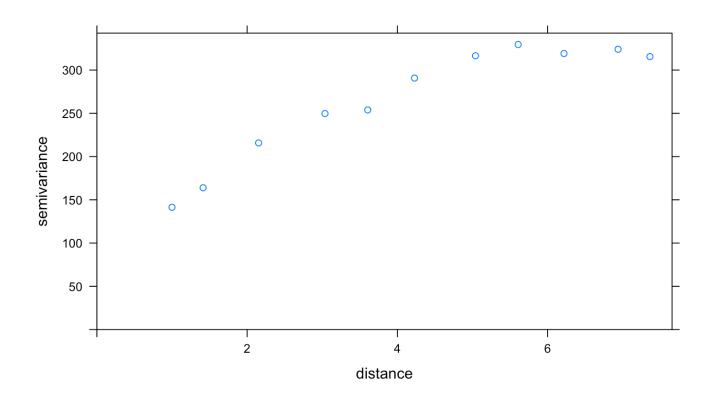
Set the maximum distance for looking at pairwise correlations:

```
max_dist <- 0.5*max(dist(coordinates(mydata_sp)))</pre>
```

Calculate a sample variogram:

The empirical variogram:

plot(semivar)



Set up models for fitting variograms:

```
vgm1 <- vgm(model = "Exp", nugget = nugget_start) # exponential
vgm2 <- vgm(model = "Sph", nugget = nugget_start) # spherical
vgm3 <- vgm(model = "Gau", nugget = nugget_start) # Gaussian</pre>
```

Fit the variogram models to the data:

```
variofit1 <- fit.variogram(semivar, vgm1)
variofit2 <- fit.variogram(semivar, vgm2)
variofit3 <- fit.variogram(semivar, vgm3)</pre>
```

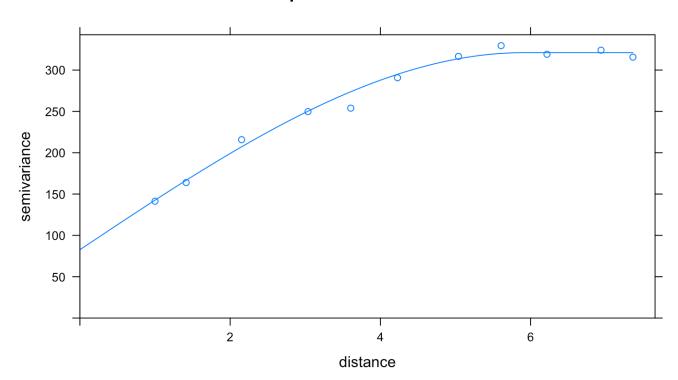
Look at the error terms to see which model is the best at minimizing error.

```
## [1] "exponential: 26857.3"
## [1] "spherical: 26058.3"
## [1] "Gaussian: 41861.0"
```

The spherical model is the best at minimizing error.

plot(semivar, variofit2, main = "Spherical model")

Spherical model



Extract the nugget and sill information from the spherical variogram:

```
nugget <- variofit2$psill[1]
range <- variofit2$range[2]
sill <- sum(variofit2$psill)
nugget.effect <- nugget/sill # the nugget/sill ratio</pre>
```

Build a correlation structure in nlme:

Update the Model:

```
lm_sph <- update(lm1, corr = cor.sph)</pre>
```

Compare Models - Log likelihood

```
logLik(lm1)
## 'log Lik.' -489.0572 (df=38)
logLik(lm_sph)
## 'log Lik.' -445.4782 (df=40)
```

Compare Models - Post-hoc Power

```
anova(lm1)[2,]

## numDF denDF F-value p-value
## cultivar 35 103 1.6411 0.029

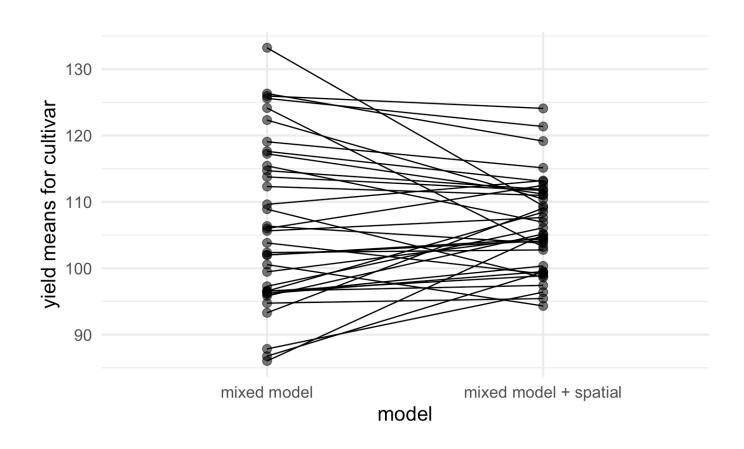
anova(lm_sph)[2,]

## numDF denDF F-value p-value
## cultivar 35 103 2.054749 0.0028
```

Compare Model Predictions

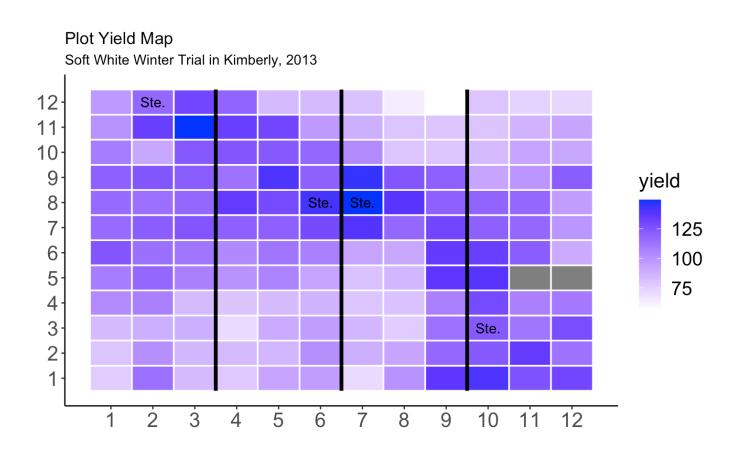
```
library(emmeans)
lme_preds <- as.data.frame(emmeans(lm1, "cultivar")) %>% mutate(model = "mixed model")
sph_preds <- as.data.frame(emmeans(lm_sph, "cultivar")) %>%
    mutate(model = "mixed model + spatial")
preds <- rbind(lme_preds, sph_preds)</pre>
```

Compare Model Predictions



Highest yielding wheat: 'Stephens' (released in 1977)

Where Was Stephens Located in the Trial?



More Notes

- When models omit blocking, the predictions may be unchanged or they may worsen. This varies by the agronomic field, but in general, blocking a field trial and including block in the statistical model improves your experimental power and controls experimental error.
- There is no single spatial model that fits all
- However, using any spatial model is usually better than none at all
- When you use spatial covariates, your estimates are better and more precise.
 This really does help you!

What's Next:

- · Track row and range information in your trial data set.
- Look at the tutorial! (we will also add SAS code)
- Try out a few models and see how it impacts your results.



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